

**MSE 480/780 – Mid-Term Exam**

**Friday, February 26<sup>th</sup>, 2:45pm, Room 3170**

Calculators may be used

No smartphones or other electronic devices may be used

One page (8.5" x 11", both sides) of handwritten notes is permitted

All writing must stop at or before 4:20pm and exam booklets handed in

**Provide all final answers clearly and unambiguously in your exam booklet.**

Total Marks: 50

*This exam has 3 pages*

**Problem 1 (25 Marks)**

A two-toothed milling cutter is being used in an up-milling operation involving two passes (a “roughing” pass followed by a “finishing” pass). Only the feed rate is changed between each pass (all other process parameters remain constant). Referring to the process geometry developed in the course, following are the parameters describing the machining operation. It may be assumed that the equivalent chip thickness ( $h_{eq}$ ) is approximately equal to the feed per tooth ( $s_t$ ) in each pass.

Depth of cut (a): 4.5mm

Entry angle ( $\Phi_1$ ): 0

Exit angle ( $\Phi_2$ ):  $\pi/3$

Swept angle of cut ( $\Phi_s$ ):  $\pi/3$  (i.e. one third-immersion)

Tool Radius (R): 15mm

Feed Per Revolution, Roughing Pass ( $s_1$ ): 0.10 mm

Feed Per Revolution, Finishing Pass ( $s_2$ ): 0.06 mm

Spindle Speed: 520 RPM

Cutting Force Constant ( $K_1$ ): 1880 N/mm<sup>2</sup>

Critical Chip Thickness ( $h^*$ ): 0.02 mm

Chip Flow Angle ( $\Psi_e$ ):  $\pi/4$

Part a (10 marks)

Plot (sketch) the corresponding cutting torque versus time for one complete revolution of the cutter (during the **roughing** pass only), clearly indicating the scale (and/or key values) of torque on your diagram.

Part b (10 marks)

The machining system’s spindle has been instrumented to measure instantaneous values of axial force ( $F_z$ ). Following are the **peak** values of axial force that were measured during the cutting operation described above:

Roughing Pass: Peak axial force ( $F_z$ ) = 243 N

Finishing Pass: Peak axial force ( $F_z$ ) = 222 N

Using this information, calculate the cutting force ratios ( $r_1, r_2$ ) for the work material / cutting tool pair.

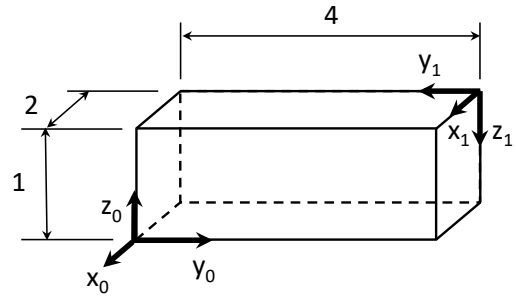
Part c (5 marks)

Ignore Part c (not covered in Spring 2018)

**Problem 2 (25 Marks)**

Part a (5 marks)

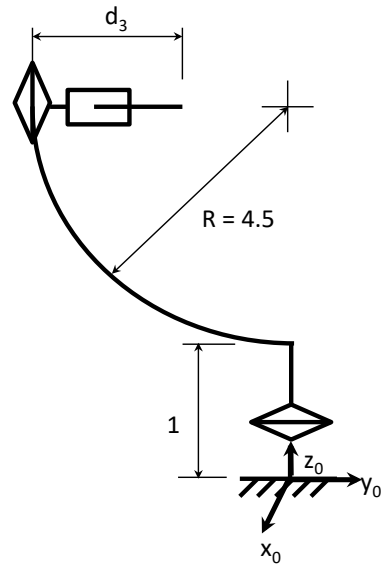
Consider the two frames ( $F_0, F_1$ ) shown to the right, with the orientation and displacement between frames as illustrated. What is the corresponding homogeneous transformation  $A_{01}$ ?



Part b (15 marks)

Consider the RRP manipulator shown to the right (with no end effector attached), which is part of an overall configuration used for satellite assembly tasks. In the starting configuration with all joint variables equal to zero (as shown), all links rest within the  $y_0z_0$  plane.

Making use of the world frame provided ( $o_0x_0y_0z_0$ ), assign frames to the manipulator following the Denavit-Hartenberg (DH) convention. Clearly list the resulting table of DH parameters and develop the homogenous transformations  $A_{01}$ ,  $A_{12}$  and  $A_{23}$ .



Part c (5 marks)

Assuming now that an end effector (gripper) is attached to the manipulator above as shown to the right (with the approach vector extending to the right and the normal vector directed out of the page), construct the final transformation matrix  $A_{3t}$

