

# Simon Fraser University

## Mechatronic Systems Engineering

Midterm Exam for  
ENSC 331: Introduction to MEMS

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**4 July 2012**

Time: 90 minutes

Name: **SOLUTIONS** \_\_\_\_\_

Student number: \_\_\_\_\_

To verify identity, each candidate should be prepared to produce, upon request, his/her Simon Fraser University Library/IO card.

All writing must be submitted with this examination booklet (notes, drafts, calculations, etc.). This booklet must not be torn or mutilated in any way, and must not be taken from the examination room.

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- copying from the work of other candidates;
- purposely exposing written papers to the view of other candidates.

Question	Mark
1	/ 20
2	/ 20
3	/ 20
4	/ 20
<b>Total:</b>	<b>/ 80</b>



Deal-Groove model for oxidation rate of silicon:	$t_{ox}^2 + At_{ox} = B(t + \tau)$
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**Deal-Groove rate constants for oxidation of (100) silicon wafers**

Temperature (°C)	A (μm)		B (μm <sup>2</sup> /hr)		τ (hr)	
	Dry	Wet	Dry	Wet	Dry	Wet
900	0.423	1.136	0.004	0.172	2.79	0.169
1000	0.232	0.424	0.010	0.316	0.616	0.036
1100	0.139	0.182	0.024	0.530	0.174	0.010

**Deal-Groove rate constants for oxidation of (111) silicon wafers**

Temperature (°C)	A (μm)		B (μm <sup>2</sup> /hr)		τ (hr)	
	Dry	Wet	Dry	Wet	Dry	Wet
900	0.252	0.676	0.004	0.172	1.72	0.102
1000	0.138	0.252	0.010	0.316	0.391	0.022
1100	0.083	0.109	0.024	0.530	0.114	0.006

**Doping profiles and surface density of dopants (x is the depth into the wafer):**

Diffusion with constant concentration of dopants at the surface	$C(x, t) = C_s \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right)$	$Q = \frac{2\sqrt{Dt}}{\sqrt{\pi}} C_s$
Diffusion with constant number of dopants at the surface	$C(x, t) = \frac{Q}{\sqrt{\pi Dt}} \exp\left(-\frac{x^2}{4Dt}\right)$	Q
Doping with implantation	$C(x) = C_p \exp\left(-\frac{(x - R_p)^2}{2\Delta R_p^2}\right)$	$Q = \sqrt{2\pi} C_p \Delta R_p$

Diffusion constant	$D = D_0 \exp\left(-\frac{E_a}{k_B T}\right)$
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Mean free path of gas molecules	$\lambda = \frac{k_B T}{\sqrt{2}\sigma P}$
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Thickness of spun photoresist	$T = K \frac{C \eta}{\omega^\alpha}$
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Resolution in proximity and contact printing	$R = \frac{3}{2} \sqrt{\lambda \left(s + \frac{T_{pr}}{2}\right)}$
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Angle between $\langle h_1 k_1 l_1 \rangle$ and $\langle h_2 k_2 l_2 \rangle$ directions	$\cos \theta = \frac{h_1 h_2 + k_1 k_2 + l_1 l_2}{\sqrt{(h_1^2 + k_1^2 + l_1^2)(h_2^2 + k_2^2 + l_2^2)}}$
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Boltzmann constant $k_B = 1.38 \times 10^{-23} \text{ J/K}$	$1\text{eV} = 1.6 \times 10^{-19} \text{ J}$
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1 atmosphere = 760 Torr = 101 325 Pa	$1\mu\text{m} = 1000\text{nm} = 10^{-4}\text{cm}$
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**The complimentary error function**

λ	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50
erfc(λ)	9.44E-1	8.88E-1	8.32E-1	7.77E-1	7.24E-1	6.71E-1	6.21E-1	5.72E-1	5.25E-1	4.80E-1
λ	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
erfc(λ)	4.37E-1	3.96E-1	3.58E-1	3.22E-1	2.89E-1	2.58E-1	2.29E-1	2.03E-1	1.79E-1	1.57E-1
λ	1.05	1.10	1.15	1.20	1.25	1.30	1.35	1.40	1.45	1.50
erfc(λ)	1.38E-1	1.20E-1	1.04E-1	8.97E-2	7.71E-2	6.60E-2	5.62E-2	4.77E-2	4.03E-2	3.39E-2
λ	1.55	1.60	1.65	1.70	1.75	1.80	1.85	1.90	1.95	2.00
erfc(λ)	2.84E-2	2.37E-2	1.96E-2	1.62E-2	1.33E-2	1.09E-2	8.89E-3	7.21E-3	5.82E-3	4.68E-3
λ	2.05	2.10	2.15	2.20	2.25	2.30	2.35	2.40	2.45	2.50
erfc(λ)	3.74E-3	2.98E-3	2.36E-3	1.86E-3	1.46E-3	1.14E-3	8.89E-4	6.89E-4	5.31E-4	4.07E-4
λ	2.50	2.55	2.60	2.65	2.70	2.75	2.80	2.85	2.90	2.95
erfc(λ)	4.07E-4	3.11E-4	2.36E-4	1.78E-4	1.34E-4	1.01E-4	7.50E-5	5.57E-5	4.11E-5	3.02E-5

**Question 1 (6+2+4+2+6 marks)**

1-I. Name three applications of silicon dioxide in MEMS fabrication and application?

- a) chemical protection
- b) Sacrificial layer
- c) Electrical isolation

1-II. E-beam lithography can be used to create features on the order of few nm. Explain why it has not replaced UV lithography in microelectronics industry?

slow speed

\_\_\_\_\_

\_\_\_\_\_

1-III. List two reasons for why a high temperature annealing of the wafer is performed after ion implantation?

- a) Drive-in the dopants
- b) Heal the crystal

1-IV. What is the major advantage of lift-off over the typical "deposition + etch" process for deposition of a metal layer on a substrate? Mention one reason only.

No metal etching / etchant is needed

1-V. List three main applications of plasma in microfabrication and the reason for its use in each of those applications.

- a) Etching (RIE): Activation of chemicals
- b) Sputtering: Ion bombardment of the target
- c) Deposition (PECVD): Lowering the reaction temperature.

**Question 2 (10+10 marks)**

We have an  $n$ -doped silicon wafer with a background concentration of  $2 \times 10^{16}$  dopants/cm<sup>3</sup>. It is required to have a junction depth of  $3\mu\text{m}$  at a Boron diffusion temperature of  $1075^\circ\text{C}$ . What is the required time under the following circumstances? For boron,  $E_a = 3.46\text{eV}$  and  $D_0 = 0.76\text{ cm}^2/\text{s}$ .

2.I. The wafer is doped using constant surface concentration method with  $10^{18}$  dopants/cm<sup>3</sup>.

Time = 25.4 Hours

$$C(x) = C_s \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right)$$

$$2 \times 10^{16} = 10^{18} \operatorname{erfc}\left(\frac{3 \times 10^{-4}}{2\sqrt{Dt}}\right) \Rightarrow \operatorname{erfc}^{-1}\left(\frac{2 \times 10^{16}}{10^{18}}\right) = 1.65$$

$$\rightarrow \sqrt{Dt} = 9.09 \times 10^{-5} \rightarrow Dt = 8.26 \times 10^{-9} \text{ cm}^2$$

$$D = 0.76 e^{\frac{-3.46 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} (273 + 1075)}} = 9.04 \times 10^{-14} \frac{\text{cm}^2}{\text{s}}$$

$$t = \frac{8.26 \times 10^{-9}}{9.04 \times 10^{-14}} = 91371 \text{ sec} = 25.4 \text{ hrs}$$

2.II. The final doping profile is Gaussian with a surface concentration of  $10^{18}$  dopants/cm<sup>3</sup>.

Time = 17.7 Hours

$$C(x) = \frac{Q}{\sqrt{\pi Dt}} e^{-\frac{x^2}{4Dt}}$$

$$C(0) = \frac{Q}{\sqrt{\pi Dt}} = 10^{18}$$

$$C(x = 3 \times 10^{-4}) = \frac{Q}{\sqrt{\pi Dt}} e^{-\frac{(3 \times 10^{-4})^2}{4Dt}}$$

$$\left. \begin{array}{l} (3 \times 10^{-4})^2 \\ 4Dt \end{array} \right\} e^{-\frac{9 \times 10^{-8}}{4Dt}} = \frac{2 \times 10^{16}}{10^{18}}$$

$$\rightarrow Dt = 5.75 \times 10^{-9} \text{ cm}^2, D = 9.04 \times 10^{-14} \frac{\text{cm}^2}{\text{s}}$$

$$t = 63606 \text{ sec} = 17.67 \text{ hrs}$$

**Question 3 (5+8+7 marks)**

We want to grow a layer of oxide on a bare <100> silicon wafer with only native oxide on it. Determine the oxide thickness under each of the following scenarios.

3-I. Wet oxidation at 1100°C for 2 hours.

$$t_{ox}: \underline{94.5} \text{ nm}$$

$$A = 0.182, B = 0.330, \tau = 0.010$$

$$t_{ox}^2 + 0.182 t_{ox} = 0.330 (2 + 0.01)$$

$$\rightarrow t_{ox} = \begin{cases} 0.945 \mu\text{m} \checkmark \\ -1.127 \mu\text{m} \end{cases}$$

3-II. Wet oxidation for 2 hours followed by dry oxidation for 22 hours, both at 1000°C.

$$t_{ox}: \underline{755} \text{ nm}$$

$$t_{ox}^2 + A_w t_{ox} = B_w (t + \tau_w)$$

$$\rightarrow t_{ox} = \begin{cases} 0.618 \mu\text{m} \checkmark \\ -1.041 \mu\text{m} \end{cases}$$

$$\begin{cases} A = 0.424 \\ B = 0.316 \\ \tau = 0.036 \end{cases}$$

$$(0.618)^2 + 0.232(0.618) = 0.010(\tau' + 0.616)$$

$$\rightarrow \tau' = 51.91 \text{ hrs}$$

$$t_{ox}^2 + 0.232 t_{ox} = 0.010 (22 + 0.616 + 51.91)$$

$$\rightarrow t_{ox} = \begin{cases} 0.755 \mu\text{m} \checkmark \\ -0.987 \mu\text{m} \end{cases}$$

3-III. Dry oxidation for 22 hours followed by wet oxidation for 2 hours, both at 1000°C.

$t_{ox}$ : ~~776~~ nm

$$t_{ox}^2 + A t_{ox} = B(t + \tau)$$

$$\begin{cases} A = 0.232 \\ B = 0.010 \\ \tau = 0.616 \end{cases}$$

$$\rightarrow t_{ox} = \begin{cases} 0.374 \mu\text{m} \checkmark \\ -0.606 \mu\text{m} \end{cases}$$

$$\rightarrow (0.374)^2 + 0.424(0.374) = 0.316(0.036 + \tau')$$

$$A = 0.424, B = 0.316, \tau = 0.036$$

$$\rightarrow \tau' = 0.908 \text{ hrs}$$

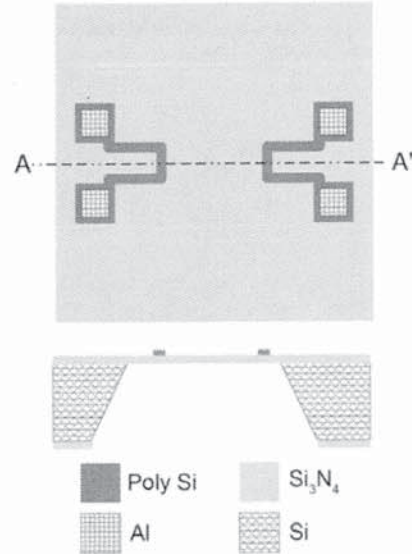
$$t_{ox}^2 + 0.424 t_{ox} = 0.316(0.908 + 0.036 + 2)$$

$$t_{ox} = \begin{cases} 0.776 \mu\text{m} \checkmark \\ -1.20 \mu\text{m} \end{cases}$$

**Question 4 (20 marks)**

Top view and cross section of a microstructure consisting of a released nitride membrane with poly silicon piezoresistors is shown to the right. Design the process flow using ONLY the following processes. Specify the orientation of the wafer that you need (i.e.,  $\langle 100 \rangle$  or  $\langle 111 \rangle$ ). If needed, use a process more than once.

- |                          |                            |
|--------------------------|----------------------------|
| • Front side lithography | • Doping                   |
| • Back side lithography  | • KOH etching              |
| • Photoresist stripping  | • XeF <sub>2</sub> etching |
| • Thermal oxidation      | • HF etching               |
| • Thermal evaporation    | • CVD of poly silicon      |
| • Sputtering             | • Silicon DRIE             |
| • Nitride CVD            | • Silicon RIE              |
| • Nitride RIE            | • Front side protection    |
| • Wet etching of Al      | • Back side protection     |



Write down the processing steps for your fabrication flow in the order they need to be performed. Do NOT provide details on chemistry, etch rate, etc. Use as few steps as needed for a reliable process. The lithography steps include all the required steps to transfer the pattern to the photoresist on the substrate (i.e., spinning, exposure, and development).

Number of masks: \_\_\_\_\_

Orientation of substrate: \_\_\_\_\_

- Step 1: Nitride CVD
- Step 2: CVD of Poly Si
- Step 3: Front side litho (Mask 1)
- Step 4: Silicon RIE
- Step 5: Photoresist stripping
- Step 6: Sputtering of Al
- Step 7: Front side litho (Mask 2)
- Step 8: wet etching of Al
- Step 9: photoresist stripping
- Step 10: Front side protection
- Step 11: Back side litho (Mask 3)
- Step 12: Nitride RIE
- Step 13: photoresist stripping
- Step 14: KOH etching
- Step 15: Removal of protective layer (release)
- Step 16: \_\_\_\_\_
- Step 17: \_\_\_\_\_
- Step 18: \_\_\_\_\_

You can use this space to answer any question with proper reference or for your calculations.